

## Rationalizing Radicals Practice

Simplify.

$$1) \frac{\sqrt{3}}{2\sqrt{5}} \cdot \frac{2\sqrt{5}}{2\sqrt{5}} = \frac{2\sqrt{15}}{4\sqrt{25}}$$

$$2) \frac{3\sqrt{4}}{2\sqrt{6}}$$

$$\frac{\sqrt{15}}{10} = \frac{2\sqrt{15}}{20}$$

$$3) \frac{\sqrt{4}}{4\sqrt{5}} \cdot \frac{4\sqrt{5}}{4\sqrt{5}} = \frac{4\sqrt{20}}{16\sqrt{25}}$$

$$4) \frac{\sqrt{2}}{\sqrt{3}}$$

$$\frac{\sqrt{5}}{10} = \frac{8\sqrt{5}}{80}$$

$$5) \frac{3}{5\sqrt{2}} \cdot \frac{5\sqrt{2}}{5\sqrt{2}} = \frac{15\sqrt{2}}{25\sqrt{4}}$$

$$6) \frac{3\sqrt{3}}{\sqrt{5}}$$

$$\frac{3\sqrt{2}}{10} = \frac{15\sqrt{2}}{50}$$

$$7) \frac{3}{\sqrt{3}}$$

$$8) \frac{5}{5\sqrt{3}}$$

## Rationalizing the Denominator

Center for Academic Support \* LRC 213 \* (816) 271-4524

## A. What It Means to Rationalize the Denominator

In order that all of us doing math can compare answers, we agree upon a common conversation, or set of rules, concerning the form of the answers.

For instance, we could easily agree that we would not leave an answer in the form of  $3 + 4$ , but would write 7 instead.

When the topic switches to that of radicals, those doing math have agreed that a **RADICAL IN SIMPLE FORM** will not (among other things) have a radical in the denominator of a fraction. We will all change the form so there is no radical in the denominator.

Now a radical in the denominator will not be something as simple as  $\sqrt{4}$ . Instead, it will have a radicand which will not come out from under the radical sign like  $\sqrt{3}$ .

Since  $\sqrt{3}$  is an irrational number, and we need to make it NOT irrational, the process of changing its form so it is no longer irrational is called **RATIONALIZING THE DENOMINATOR**.

## B. There are 3 Cases of Rationalizing the Denominator

1. **Case I:** There is **ONE TERM** in the denominator and it is a **SQUARE ROOT**.

Example:  $\frac{7}{\sqrt{3}}$

Labels: "square root" points to  $\sqrt{3}$ ; "one term" points to 7.

\*Procedure: Multiply top and bottom by the same radical.

$$\frac{7}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{7\sqrt{3}}{3}$$

Look at what is happening here!  
 $(\frac{7}{\sqrt{3}}) \cdot \sqrt{3}$   
 Since squaring is the opposite of taking the square root, they cancel each other, leaving the 3.

*found on the bottom*