

What you need to know and be able to do	Things to Remember	Problem	Problem
1. Justify steps using properties	Associative prop Commutative prop Symmetric prop Add property of = Subtract prop of = Division prop of = Mult prop of = Distributive prop	$14 = 5x - (2x + 4)$ $14 = 5x - 2x - 4$ $14 = 3x - 4$ $18 = 3x$ $6 = x$ $X = 6$	<u>original problem</u> <u>Distributive Property</u> <u>Assoc. - combine like</u> <u>Add POE</u> <u>Div POE</u> <u>Symmetric POE</u>
2. Solve multi-step equations and inequalities	If variables cancel and left with false statement ( $4 = 6$ ), then no solution. If true statement ( $4=6$ ) then infinitely many solutions.  Flip the $<$ $>$ sign when multiplying or dividing by a negative	a. $-4(2x - 3) = -6x - 12$ $-8x + 12 = -6x - 12$ $+6x \quad +6x$ $-2x + 12 = -12$ $-12 \quad -12$ $-2x = -24$ $\boxed{x = 12}$  b. $3x + 12 = -4(-6x - 3) + 3x$ $3x + 12 = 24x + 12 + 3x$ $3x + 12 = 27x + 12$ $-3x \quad -3x$ $12 = 24x + 12$ $-12 \quad -12$ $0 = 24x$ $\boxed{x = 0}$	c. $-4x - (2x + 12) > 3x + 6$ $-4x - 2x - 12 > 3x + 6$ $-6x - 12 > 3x + 6$ $+6x \quad +6x$ $-12 > 9x + 6$ $-6 \quad -6$ $-18 > 9x$ $\boxed{x < -2}$  d. $x - 7x - 4 \geq 10$ $-6x - 4 \geq 10$ $+4 \quad +4$ $-6x \geq 14$ $x \leq -\frac{14}{6}$ $\boxed{x \leq -\frac{7}{3}}$
3. Solve literal equations (rearrange formulas)	Isolate the variable  Multiply by the denominator when there is a fraction	a. solve for p if $N = \frac{p}{m} \cdot m$ $Nm = p$	b. solve for W if $P = \frac{2}{2}(L + W)$ $\frac{P}{2} = L + W$ $\frac{P}{2} - L = W$
4. Combining functions and function notation	Add: combine like terms Subtract: distribute negative Multiply: add exponents  Evaluate: substitute a number for x	$f(x) = x^2 + 3x - 5$ $g(x) = 2x^2 - x + 2$ $h(x) = 3x^3$  a. $f(x) + g(x)$ $x^2 + 3x - 5 + 2x^2 - x + 2$ $\underline{\underline{+}} \quad \underline{\underline{+}}$ $3x^2 + 2x - 3$	b. $f(x) - g(x)$ $x^2 + 3x - 5 - (2x^2 - x + 2)$ $x^2 + 3x - 5 - 2x^2 + x - 2$ $\underline{\underline{-}} \quad \underline{\underline{-}}$ $-x^2 + 4x - 7$  c. $f(2) + h(2) \rightarrow 5 + 24 = 29$ $f(2) = (2)^2 + 3(2) + 5$ $= 4 + 6 - 5$ $= 10 - 5$ $= 5$ $h(2) = 3(2)^3$ $= 3(8)$ $= 24$

## 5. Arithmetic Sequences

Adding or Subtracting to get to the next term

$$f(n) = dn + z$$

$$a_n = a_{n-1} + d$$

$$a_n = a_1 + d(n-1)$$

a.

Write the rule for the following sequence and find the 50<sup>th</sup> term:  
 3, 6, 9, 12, 15, 18

Specific  $\rightarrow$  Explicit

$$a_n = 3 + 3(n-1)$$

$$a_n = 3 + 3n - 3$$

$$\boxed{a_n = 3n}$$

$$a_{50} = 3(50) = 150$$

b.

Write the first 4 term in the sequence:

$$a_1 = -2 \quad a_3 = 1 \quad a_5 = -3$$

$$a_2 = 3 \quad a_4 = -1$$

c. write an explicit formula for the table:

x	1	2	3	4
y	2	5	8	11

$$a_n = 2 + 3(n-1)$$

$$a_n = 2 + 3n - 3$$

$$\boxed{a_n = 3n - 1}$$

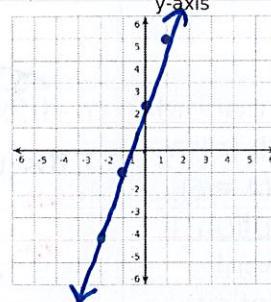
## 6. Graph linear functions (lines)

Write equation in slope intercept form by solving for y  
 $y = mx + b$

b is y-intercept and m is slope (rise over run)

vertical lines:  
 $x =$  a number and undefined slope  
 horizontal lines:  
 $y =$  a number and has a slope of zero

graph  $3x - y = -2$



$$y = mx + b \leftarrow \text{NEEN}$$

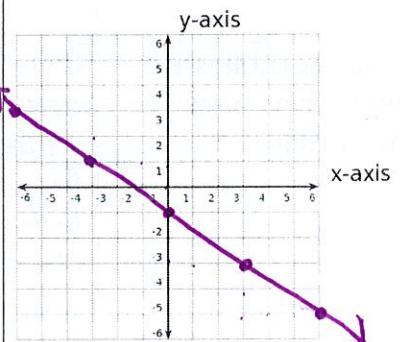
$$3x - y = -2$$

$$-3x \quad -3x$$

$$\frac{-y}{-1} = \frac{-3x}{-1} - \frac{2}{-1}$$

$$\boxed{y = 3x + 2}$$

Graph  $y = -\frac{2}{3}x - 1$



## 7. solve word problems

Consecutive integer: use  $x, x + 1, x + 2, \dots$

Consecutive even AND odd: use  $x, x + 2, x + 4, \dots$

Perimeter: draw rectangle and label sides (let  $x$  equal shortest side)

Average: add all numbers plus  $x$  and divide by number you have

a. find 3 consecutive odd integers that add up to 309. Find the integers.

$$\underline{x} + \underline{x+2} + \underline{x+4}$$

$$3x + 6 = 309$$

$$3x = 303$$

$$x = 101$$

101  
103  
105

b. find 4 consecutive integers that add up to 130.

31, 32, 33, 34

$$\underline{x} + \underline{x+1} + \underline{x+2} + \underline{x+3}$$

$$4x + 6 = 130$$

$$4x = 124$$

$$x = 31$$

c. The length of a rectangle is 3 more than twice the width. Find length and width if the perimeter is 48.

$$\begin{aligned} L &= 3 + 2W \\ P &= 2L + 2W \\ 48 &= 2(3 + 2W) + 2W \end{aligned}$$

$$\begin{aligned} 48 &= 6 + 4W + 2W \\ 48 &= 6 + 6W \\ 42 &= 6W \\ 7 &= W \end{aligned}$$

d. Bentley buys pokemon cards for \$5 a pack with a service charge of \$1.50. Write an equation to represent Bentley's spending.

$$y = 5x + 1.50$$

↑ cost per pack  
 ↑ initial amt

## 8. describe characteristics of linear functions

Domain: all x values

Range: all y values

X intercept:  
where line crosses x axis;  
where  $y = 0$ .

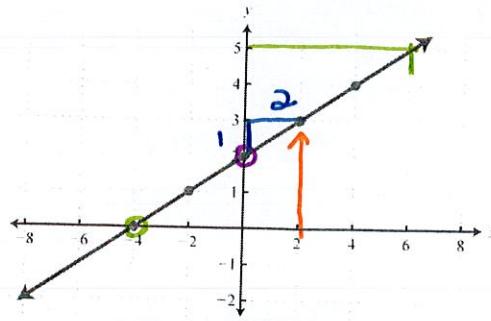
$y = mx + b$  ←  
Y intercept:  
where line crosses y axis;  
where  $x = 0$

End behavior:

As  $x \rightarrow \infty$ ,  $f(x)$

→ \_\_\_\_\_

As  $x \rightarrow -\infty$ ,  
 $f(x) \rightarrow$  \_\_\_\_\_



Eqn of line:  $y = 1/2x + 2$

✗ Domain:  $(-\infty, \infty)$

✗ Range:  $(-\infty, \infty)$

✗ Y intercept:  $(0, 2)$

✗ X intercept:  $(-4, 0)$

✗  $F(2) = 3$

✗ If  $f(x) = 5$ , then  $x = 6$

✗ End behavior:

As  $x \rightarrow +\infty$   $y \rightarrow \infty$

As  $x \rightarrow -\infty$   $y \rightarrow -\infty$