

Name: \_\_\_\_\_

Date: \_\_\_\_\_ Class Period: \_\_\_\_\_

### Composition of Transformations Notes

A composition of transformations is just a fancy way to represent a combination of transformations.

We see compositions of transformations in function notation.

### Composition of Transformations Notation:

$$f(x) = g(h(x))$$

How to perform the transformations:

\* -Always perform the transformation that is inside parenthesis first. This is the one you see in the very middle. It is also the first one you see if you read from right to left.

-Next, take the result of the transformation inside parenthesis and apply the next transformation (the one that is to the left of the inside parenthesis).

\* if transformations are written Read: L → R or Up to Down

Example: Describe the sequence that you will perform the composition of transformations:

1.  $S(x, y) = R_{90^\circ}(R_{y=x}(x, y))$   
2nd 1st Reflection over  $y=x$   $A'$   
 $A' \rightarrow$  Rotate 90 CCW  $A''$

2.  $A(x, y) = R_{x\text{-axis}}(T_{5,-1}(x, y))$   
2nd 1st Translate RS, D1  $A'$   
 $A' \rightarrow$  Reflect over x axis  $A''$

3.  $Y(x, y) = T_{4,7}(T_{-3,0}(x, y))$   
2nd 1st Translation L3  $Y'$   
 $Y' \rightarrow$  Translation R4, U7  $Y''$

4.  $W(x, y) = R_{y=-x}(R_{270^\circ}(x, y))$   
2nd 1st Rotation 90 CCW  $W'$   
 $W' \rightarrow$  Reflection over  $y=-x$   $W''$

5.  $H(x, y) = R_{y=2}(R_{x=-3}(x, y))$   
2nd 1st Reflection over  $x=-3$   $H'$   
 $H' \rightarrow$  Reflection over  $y=2$   $H''$

6.  $A(x, y) = T_{-2,-8}(R_{y\text{-axis}}(R_{180^\circ}(x, y)))$   
3rd 2nd 1st Rotation 180 CCW  $A'$   
 $A' \rightarrow$  Reflection over y axis  $A''$   
 $A'' \rightarrow$  Translate L2 D8  $A'''$

7.  $T(x, y) = R_{x=5}(R_{270^\circ}(R_{90^\circ}(R_{y=x}(R_{-90^\circ}(T_{0.5,-2.3}(x, y))))))$   
1st 2nd 3rd 4th 5th

Rotation 180 CCW  $A'$   
 $A' \rightarrow$  Reflection over y axis  $A''$   
 $A'' \rightarrow$  Translate L2 D8  $A'''$

Translate R.5 D2.3  $T'$

$T''''$  Rotate 90 CCW  $T'''''$

$T'''''$  Rotate 90 CW  $T''''''$

$T'$  Rotate 90 CW  $T''$   
 $T''$  Reflected over  $y=x$   $T'''$

$T''''''$  Reflect over  $x=5$   $T'''''''$